

2022-23

Discrete Mathematical Structures

MAO441

Full Marks:25

Time: One Hour Thirty Minutes

Answer any five questions (5x5=25)

1. Define indirect Proof and then prove by induction $1+2+\dots+(2k-1)=k^2$. Define Proof by Contraposition.
2. Let $\{a_n\}$ be a sequence of natural numbers such that $a_1=5$, $a_2=13$ and $a_{n+2}=5a_{n+1}-6a_n$ for all natural numbers n . Prove that $a_n=2^n+3^n$.
3. Prove that $2^n > n^2$ for all natural numbers $n \geq 5$ using Induction.
4. Write "Warshall's" algorithm to find out the transitive closure of a relation.
5. Write the equivalent form of "p implies q" and "p if and only if q". Define Tautology, Contradiction with example.
6. Define an equivalence relation. Let R is a relation on a set of integers such that aRb is ' $a=b$ ' a, b are integers, is the relation R is an equivalence relation?
7. If A is a set such that $A=\{1,2,3,4\}$ and R_1 is a relation $R_1=\{(1,1), (2,3), (2,2), (1,3)\}$, find out reflexive and symmetric closures of this relation. Define transitive closure of a relation with example.